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### Venn Diagram and Set Operations

#### **Objectives:**

After reading and completing this module, you will be able to do these:

- ✓ Show relationships between and among sets using Venn Diagram i.e. union, intersection and complementation.
- Define relationships between and among sets given in Venn diagram i.e. intersection and union of sets.



#### VENN DIAGRAM

 The Venn diagram, named after the English logician James Venn, is a pictorial representation involving relations between and among the sets. It consists of a rectangle that represents the universal set and circles that represent the subsets.

#### **UNIVERSAL SET**

• The Universal set, or the **universe**, denoted by **U**, is the set that contains all elements being discussed in a given discussion.

#### Example 1

Given: Universal set **U** with its subsets A and B.

#### Example 2

Given:

**U** = { s, w, x, y, z} A = { s, x, y, x }





#### Union of Sets

The union of two sets A and B, written A U B, is the set of all elements in A or in B. That is, A U B = {  $x | x \in A \text{ or } B$  }.



#### Example 3

Given: V = { 5, 8, 11, 14, 27} W = { 1, 2, 3, 4} Find: V U W



Answer: V U W = {1, 2, 3, 4, 5, 8, 11, 14, 17}

#### Example 4

Given:  $G = \{2, 3, 4, 5\}$ H =  $\{3, 6, 9, 12\}$ Find: G U H

Answer: G U H = {2, 3, 4, 5, 6, 9, 12}

#### **Intersection of Sets**

The intersection of two sets A and B, written A  $\cap$  B, is the set of all elements common to both A and B. That is, A  $\cap$  B = {x | x \in A and x \in B}.



#### Example 5

Given: G =  $\{2, 3, 4, 5\}$ H =  $\{3, 6, 9, 12\}$ Find: G  $\cap$  H Answer: G  $\cap$  H =  $\{3\}$ 

#### **Complement of a Set**

The complement of set A, denoted by A' (read as A prime) or Ac, is the set of all elements in the universal set U that are not in A. That is,  $A' = \{x \mid x \in U \text{ and } x \notin A\}$ .

#### Example 6

Given: U = {4, 5, 7, 8, 10, 11, 13, 14, 16, 17} V = {5, 8, 11, 14, 17}

Find: V' or Vc

Answer: V' = {4, 7, 10, 13, 16}



#### Example 7

Given:  $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$   $A = \{2, 4, 6, 8, 10, 12\}$   $B = \{1, 3, 5, 7, 9, 11\}$   $C = \{4, 8, 12\}$ Find: A U B  $A \cap C$  B C C'(A U B)'

Answer:

A U B =  $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$ A  $\cap$  C =  $\{4, 8, 12\}$ B U C =  $\{1, 3, 4, 5, 7, 8, 9, 11, 12\}$ C' =  $\{1, 2, 3, 5, 6, 7, 9, 10, 11\}$ (A U B) **' = \{** 







Union



Intersection

